

# Section 10.5 - Transformations and 3D Geometry

Name: \_\_\_\_\_ Class: \_\_\_\_\_

## Video Notes

### Transformations

<u>Reflections</u>	<u>Translations</u>	<u>Dilations</u>	<u>Rotations</u>
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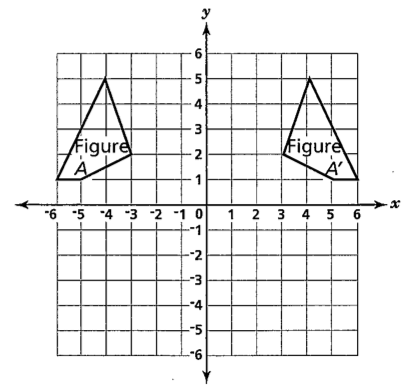
### Examples

<p style="text-align: center;"><b>Example 1</b></p> <p>Describe a sequence of transformations that maps triangle C to triangle D.</p>	<p style="text-align: center;"><b>Example 2</b></p> <p>Describe a sequence of transformations that maps triangle E to triangle G.</p>
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### 3D Geometry – Volume

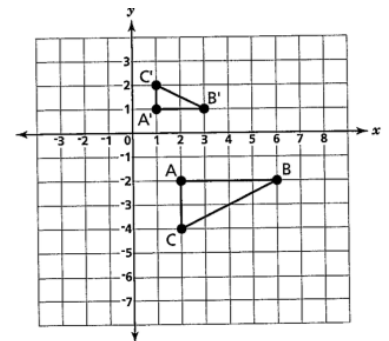
Cylinder $V = \pi r^2 h$	Cone $V = \frac{1}{3} \pi r^2 h$	Sphere $V = \frac{4}{3} \pi r^3$
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1.) Figure A and its image after a transformation, Figure A', are shown in the coordinate plane below. The two figures are congruent. How was Figure A transformed to create the congruent Figure B?



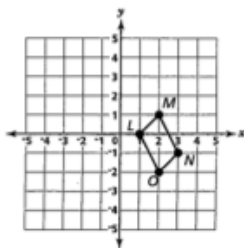
- (A) It was reflected over the x-axis.
- (B) It was reflected over the y-axis.
- (C) It was translated 9 units to the right.
- (D) It was rotated 90° clockwise around the origin.

2.) The two triangles shown are similar. Which series of transformations could have been used to transform triangle ABC to similar triangle A'B'C'?

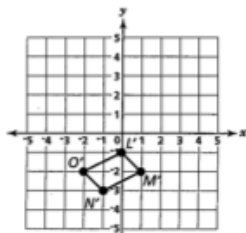


- (A) a dilation about the origin with a scale factor of 0.25 and a reflection across the y-axis.
- (B) a dilation about the origin with a scale factor of 0.5 and a reflection across the y-axis.
- (C) a dilation about the origin with a scale factor of 0.25 and a reflection across the x-axis.
- (D) a dilation about the origin with a scale factor of 0.5 and a reflection across the x-axis.

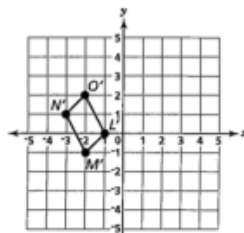
3.) Parallelogram LMNO is shown below.



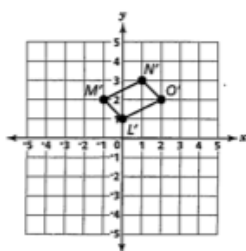
Which figure represents parallelogram LMNO rotated 90° counterclockwise around the origin?



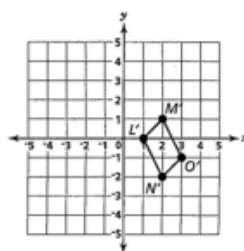
A



C



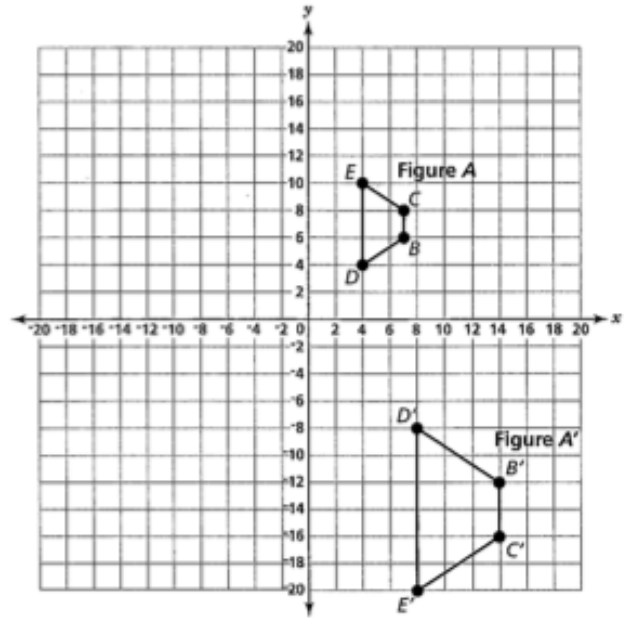
B



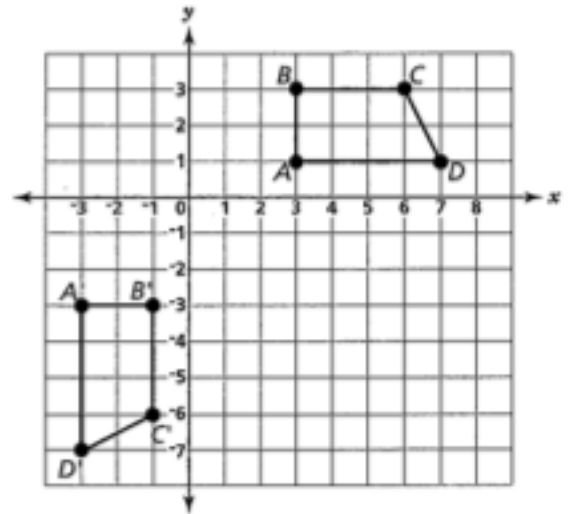
D

**Go On**

- 4.) Which sequence of transformations on Figure A will generate the similar images, figure A', as shown on the coordinate plane below?
- (A) Dilate Figure A by a scale factor of 2 and with a center of dilation at the origin, and reflect it across the y-axis.
  - (B) Dilate Figure A by a scale factor of 2 and with a center of dilation at the origin, and reflect it across the x-axis.
  - (C) Dilate Figure A by a scale factor of 4 and with a center of dilation at the origin, and rotate it  $90^\circ$  clockwise around the origin.
  - (D) Dilate Figure A by a scale factor of 4 and with a center of dilation at the origin, and rotate it  $180^\circ$  clockwise around the origin.



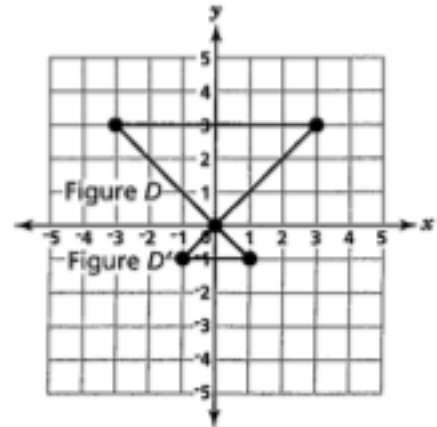
- 5.) Which sequence of transformations was used to create quadrilateral A'B'C'D'?
- (A) Quadrilateral ABCD was rotated  $90^\circ$  counterclockwise about the origin and then translated 4 units down.
  - (B) Quadrilateral ABCD was rotated  $270^\circ$  counterclockwise about the origin and then translated 4 units left.
  - (C) Quadrilateral ABCD was reflected across the x-axis and then rotated  $270^\circ$  counterclockwise about the origin.
  - (D) Quadrilateral ABCD was reflected across the x-axis and then rotated  $90^\circ$  counterclockwise about the origin.



- 6.) A water tank is in the shape of a circular cylinder with a height of 10 feet and a volume of  $90\pi$  cubic feet. What is the diameter, in feet, of the water tank?
- (A) 9
  - (B) 5
  - (C) 3
  - (D) 6

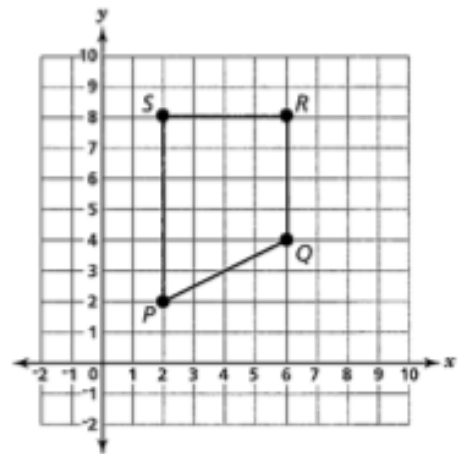
7.) In the coordinate plane below, Figure D' is similar to Figure D. Which two transformations were performed on figure D resulting in figure D'?

- (A) A reflection over the x-axis and dilation by a scale factor of  $\frac{1}{2}$
- (B) A reflection over the x-axis and dilation by a scale factor of  $\frac{1}{3}$
- (C) A dilation with a scale factor of  $\frac{1}{2}$  and a reflection over the y-axis
- (D) A dilation with a scale factor of  $\frac{1}{3}$  and a reflection over the y-axis



8.) Look at figure PQRS. If figure PQRS is dilated using a scale factor of 0.5 with the center of dilation at (0,0), what are the coordinates of the points of the image P'Q'R'S'?

- (A) P'(1.5,1.5), Q'(2.5,1.5), R'(2.5,3.5), S'(0.5,3.5)
- (B) P'(2.5,2.5), Q'(6.5,4.5), R'(6.5, 8.5), S'(2.5,8.5)
- (C) P'(4,4), Q'(12,8), R'(12,16), S'(4,16)
- (D) P'(1,1), Q'(3,2), R'(3,4), S'(1,4)

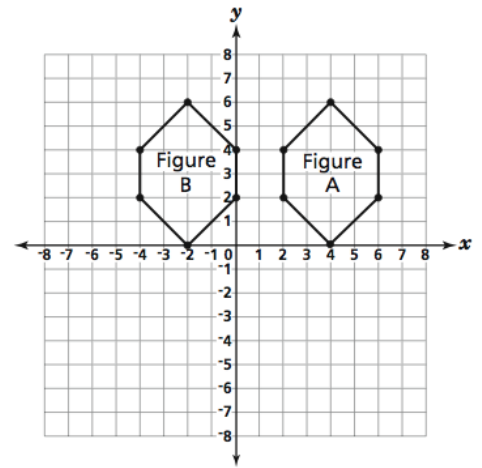


9.) Triangle ABC was rotated  $90^\circ$  clockwise. Then it underwent a dilation centered at the origin with a scale factor of 4. Triangle A''B''C'' is the resulting image.

a.) What parts of  $\Delta A''B''C''$  are congruent to the corresponding parts of the original triangle? Explain your reasoning. **(3 points)**

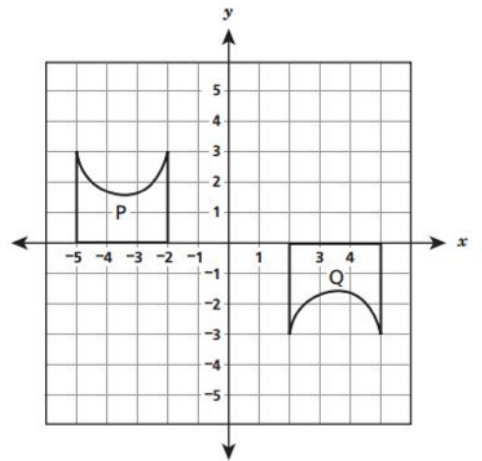
b.) Compare the perimeters of  $\Delta ABC$  and  $\Delta A''B''C''$ . Explain your reasoning. **(3 points)**

10.) If Brandon drew two figures on the coordinate grid shown below, which transformation did Brandon apply to Figure A to get Figure B?



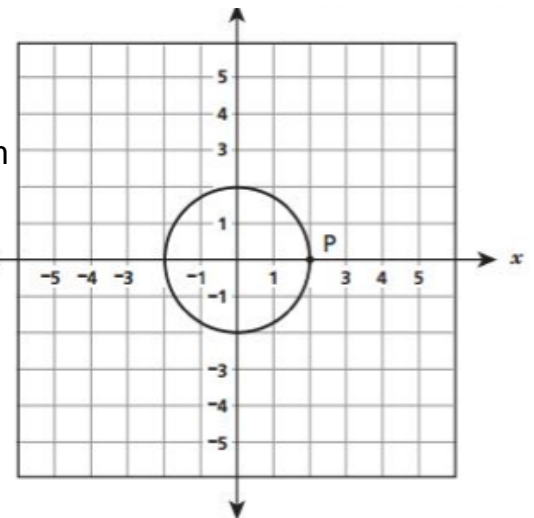
- (A) rotated  $90^\circ$
- (B) dilated by 6
- (C) reflected in the y-axis
- (D) translated 6 units to the left

11.) Figure Q was the result of a sequence of transformations on figure P, both shown below. Which sequence of transformations could take figure P to figure Q?



- (A) reflection over the x-axis and translation 7 units right
- (B) reflection over the y-axis and translation 3 units down
- (C) translation 1 unit right and  $180^\circ$  rotation about the origin
- (D) translation 4 units right and  $180^\circ$  rotation about the origin

12.) The circle shown below is centered at  $(0,0)$  and passes through point P located at  $(2,0)$ . The circle is dilated with the center of dilation at the origin and a scale factor 0.5 and then translated up 3 units. What are the coordinates of the image of point P after this transformation?



- (A)  $(4,3)$
- (B)  $(1,3)$
- (C)  $(1,1.5)$
- (D)  $(0.5,3)$

13.) Rectangle R undergoes a dilation with scale factor  $\frac{1}{4}$  and then a reflection over the y-axis. The resulting image is Rectangle S. Which statement about Rectangles R and S is true?

- (A) They are congruent and similar.
- (B) They are similar but not congruent.
- (C) They are congruent but not similar.
- (D) They are neither congruent nor similar.

14.) Find the **exact** volume of a cylinder that has a radius of 7 and a height of 10.

15.) Find the volume of a cone that has a diameter of 10 inches and a height of 13 inches. Round to the nearest hundredth.

16.) Find the volume of a sphere that has a diameter of 22 cm. Round to the nearest whole number.

17.) A box contains 9 identical glass spheres that are used to make snow globes. The spheres are tightly packed, as shown below. What is the total volume, in cubic inches, of all 9 spheres? Round your answer to the nearest tenth of a cubic inch.

