

# Unit 7 Notes

## 3D Geometry - Volume of Cylinders, Cones, and Spheres



### Tentative Schedule

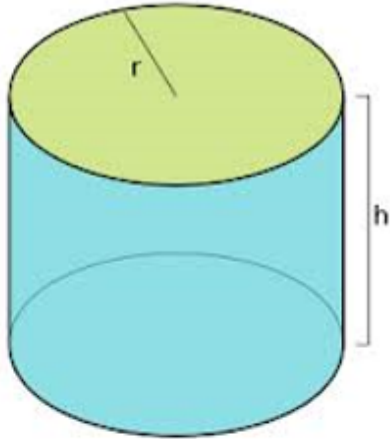
Day	Classwork	Assignment
Thurs. 2/26	<b>Test #6</b>	Video #7.1: 3D Geometry Day 1 with Notes 7.1
Fri. 2/27 Mon. 3/2	P.S. #7.1	Video #7.2: 3D Geometry Day 2 with Notes 7.2
Tues. 3/3	P.S. #7.2	Finish P.S. #7.2 and Optional Review Sheet
Wed. 3/4 Thurs. 3/5	<b>Quiz #7</b>	TBD

**Name:** \_\_\_\_\_

# Notes 7.1 - 3D Geometry Day 1

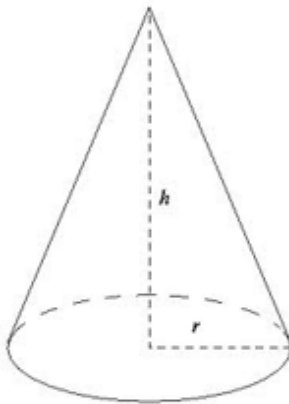
## Volume Formulas

Cylinder



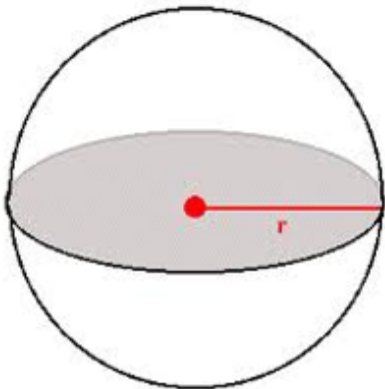
$$V = \pi r^2 h$$

Cone



$$V = \frac{1}{3} \pi r^2 h$$

Sphere



$$V = \frac{4}{3} \pi r^3$$

- 1.) Find the volume of a cylinder that has a height of 30 inches and a radius of 4 inches. Express your answer in two ways: as an exact answer and rounded to the nearest whole number.

$$V = \pi r^2 h$$

$$V = \pi (4)^2 (30)$$

$$V = \pi (16)(30)$$

$$V = 480\pi \text{ in}^3 \approx \underline{\underline{1507.96447372 \dots}}$$

Exact Answer:  $480\pi \text{ in}^3$

Nearest Whole Number:  $1508 \text{ in}^3$

- 2.) Find the volume a cone that has a height of 30 inches and a radius of 4 inches. Express your answer as an exact answer.

$$V = \frac{1}{3}\pi r^2 h$$

$$V = \frac{1}{3}\pi (4)^2 (30)$$

$$V = \frac{1}{3}\pi (16)(30)$$

$$V = \frac{1}{3}\pi (480)$$

exact:

$$V = 160\pi \text{ in}^3$$

- 3.) Find the volume of a sphere that has a radius of 3 inches. Round to the nearest thousandth.

$$V = \frac{4}{3}\pi r^3$$

$$V = \frac{4}{3}\pi (3)^3$$

$$V = \frac{4}{3}\pi (27) \rightarrow \frac{27 \cdot 4}{1 \cdot 3} = 36$$

$$V = 36\pi \approx \underline{\underline{113.097335529 \approx 113.100 \text{ in}^3}}$$

## Notes 7.2 - 3D Geometry Day 2

1.) Find the volume of a perfect sphere that has a radius of  $9 \cdot 10^5$  units.

$$r = 9 \cdot 10^5$$

$$V = \frac{4}{3}\pi r^3$$

$$V = \frac{4}{3}\pi(9 \cdot 10^5)^3 \rightarrow (9 \cdot 10^5)^3 = 9^3 \cdot (10^5)^3 \quad \frac{81}{129}$$

$$V = \frac{4}{3}\pi(729 \cdot 10^{15})$$

$$V = 972\pi \cdot 10^{15} \approx 3054 \cdot 10^{15} = 3.054 \cdot 10^3 \cdot 10^{15} = \boxed{3.054 \cdot 10^{18} \text{ un}^3}$$

2.) Find the volume of a cylinder that has a radius of  $4.7 \cdot 10^5$  and a height of  $3.6 \cdot 10^4$ .

$$r = 4.7 \cdot 10^5$$

$$h = 3.6 \cdot 10^4$$

$$V = \pi r^2 h$$

$$V = \pi(4.7 \cdot 10^5)^2 \cdot (3.6 \cdot 10^4)$$

$$V = \pi(22.09 \cdot 10^{10})(3.6 \cdot 10^4)$$

$$V \approx 249.8 \cdot 10^{14} = 2.498 \cdot 10^2 \cdot 10^{14} = \boxed{2.498 \cdot 10^{16} \text{ un}^3}$$

3.) Find the combined volume of two spheres: one that has a radius of  $3.1 \cdot 10^4$  units and another that has a radius of  $6.7 \cdot 10^3$ .

sphere 1

sphere 2

sphere 1:

$$V = \frac{4}{3}\pi r^3$$

$$V = \frac{4}{3}\pi(3.1 \cdot 10^4)^3$$

$$V = \frac{4}{3}\pi(29.791 \cdot 10^{12})$$

$$V = 124.788 \cdot 10^2$$

$$V = 1.25 \cdot 10^2 \cdot 10^2$$

$$V = 1.25 \cdot 10^4 \text{ un}^3$$

sphere 2:

$$V = \frac{4}{3}\pi r^3$$

$$V = \frac{4}{3}\pi(6.7 \cdot 10^3)^3$$

$$V = \frac{4}{3}\pi(300.763 \cdot 10^9)$$

$$V = 1259.83 \cdot 10^9$$

$$V = 1.26 \cdot 10^3 \cdot 10^9$$

$$V = 1.26 \cdot 10^{12}$$

Combined volume:

$$1.25 \cdot 10^{14} + 1.26 \cdot 10^{12}$$

$$1.25 \cdot 10^{14} + .0126 \cdot 10^{14}$$

$$\begin{array}{r} 1.2500 \\ + 0.0126 \\ \hline 1.2626 \end{array}$$

$$\boxed{1.2626 \cdot 10^{14} \text{ un}^3}$$

FINAL ANSWER